Thrust from the magnetic nozzle helicon plasma thruster

Kazunori Takahashi¹⁻³⁾, Christine Charles¹⁾, Rod Boswell¹⁾

- 1) Space Plasma, Power and Propulsion Laboratory, The Australian National University
 - 2) Department of Electrical Engineering, Iwate University
 - ³⁾ Soft-Path Engineering Research Center, Iwate University

I. INTRODUCTION

The momentum flux delivered by charged particles in plasmas and its interaction with magnetic fields have been significant subjects associated with astrophysical jets [1], magnetospheric physics [2], thermonuclear fusion devices [3], and electric propulsion systems [4]. It is essential to understand and characterize the gain/loss mechanisms of the momentum flux for clarifying the acceleration/confinement processes of charged particles in nature and in terrestrial plasma devices. For instance, acceleration processes in current-driven plasmas such as applied-field magneto-plasma-dynamic arcjet plasmas have been investigated [5, 6]. Recent theoretical studies concerning the spontaneous formation of electric double layers (DLs) have shown that no additional net momentum is delivered by the DLs [7, 8]. Instead, one- and two-dimensional theories have shown enhancements of the net axial force [7, 9] from an expanding cross section or an expanding magnetic field (called thrust in the field of electric propulsion), even in current-free plasmas such as radiofrequency (rf) inductively-coupled or helicon mode discharges. Direct measurements of the net force from magnetically expanding current-free plasmas are presently under investigation [10–12]; recently an experiment focused on the role of the expanding magnetic field on the gain/loss of the axial force in current-free plasmas has been reported briefly [13]. Here the axial force imparted from the magnetically expanding current-free plasma is directly measured for three different experimental configurations and compared with a two-dimensional fluid theory.

II. EXPERIMENTAL SETUP

Experiments are performed within the *Irukandji* vacuum chamber at the Australian National University (ANU), which is 100 cm in diameter and 140 cm in length and is pumped down to a base pressure of about 10^{-6} Torr. Two rf plasma source systems with an expanding magnetic field are presently used. Figure 1(a) shows a schematic of the first source (custom built at ANU), which has a 25-cm-long, 9-cm-inner-diameter pyrex source tube and an expanding magnetic field applied by using a combination of two axial solenoids located at z=-5.5 cm (downstream current, I_{Bdown}) and -18.5 cm (upstream current, I_{Bup}), where the open exit of the source tube is defined as z=0. Axial profiles of the magnetic field B_z on axis for solenoidal currents (I_{Bup}, I_{Bdown}) of (6A, 6A) and (0A, 6A) are plotted in Fig. 2(a) and labeled 'A mode' and 'B mode', respectively. Topologies of the field lines are also drawn in Fig. 2(b). Argon gas is fed into the source tube via a small ceramic tube which is mechanically isolated from the source tube (Fig. 1(a)). The flow rate is maintained at 25 sccm which gives a pressure within the chamber of about 1 mTorr. An rf loop antenna (\sim 11-cm-inner-diameter and 2 turns) is located at z=-12cm and is mechanically isolated from the source tube. The second source is a permanent magnet (PM) expanding source (custom built at Iwate University) [11], with a similar structure as that shown on Fig. 1(a): briefly, the PM source has a 6.5-cm-inner-diameter, 8-cm-long source tube (the cavity length is adjusted using a movable insulating plate located at the closed end of the source) and a combination of two concentric neodymium iron boron PM arrays providing an expanding magnetic field shown in Fig. 2(a) and 2(b) (labeled 'C mode').

The rf loop antenna (\sim 8-cm-inner-diameter and 2 turns) is located at z=-4.5 cm. For both sources the antennas are powered from a 13.56 MHz rf power generator through an impedance matching circuit.

The solenoids or PMs are attached to the force balance immersed within the Irukandji vacuum chamber and their displacement (generated when initiating the plasma) is measured using a high-resolution laser-displacement sensor (resolution: 0.1 μ m, sampling rate: 312.5 Hz) [11]. No displacement is detected when the cold gas is introduced; the force by the neutral gas is negligible in the present experiments. The laser system is initially operated with flowing

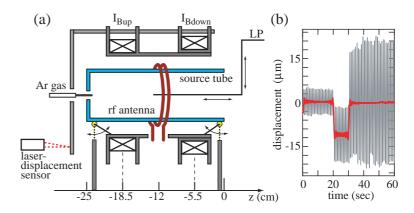


FIG. 1: (a) Schematic of the experimental setup. (b) Typical displacement signal from the force balance.

gas and no plasma for a period of 20 s; the rf power and argon plasma are subsequently turned on for about 10 s. After the plasma is turned off, the data is taken for another 30 s. A typical signal of the displacement is plotted in Fig. 1(b) as a thin line. As forces applied to the balance result in an oscillation of the pendulum with a frequency of about 1 Hz as shown in Fig. 1(b), the data is filtered to remove the pendulum oscillation [bold line in Fig. 1(b)]. The displacement corresponds to the difference between the positions measured during the 'plasma off' and 'plasma on' periods. The force imparted by the plasma is obtained using the calibration coefficient relating the displacement to the force (typically, 0.5-0.6 mN/ μ m for the 'A and B modes', and 0.35 mN/ μ m for the 'C mode'), which can be obtained as described in Ref [11]. For the 'A and B modes' of the first source, the measurement of the axial forces are performed when the source tube is attached either to the solenoids or to the Irukandji vacuum chamber. These two distinct configurations respectively lead to the direct measurements of the total force T_{total} resulting from both the source tube and magnetic field, and of the force T_B resulting solely from the magnetic field. For the 'C mode' of the second source, the source tube is attached to the array of PMs and only the measurement of T_{total} is obtained. The local plasma density $(n_i = n_e = n)$ and electron temperature T_e are measured with a radially and axially movable Langmuir probe (LP), assuming a Maxwellian electron energy distribution, and using Sheridan's sheath expansion model [14].

III. EXPERIMENTAL AND ANALYTICAL RESULTS

Figure 2(c) shows the normalized electron pressure $(p_e = nk_BT_e)$ derived from the plasma density n and electron temperature T_e measured along the z axis, where k_B is the Boltzmann constant.

The axial positions z_0 having the maximum electron pressure are at $z_0 = -17$ cm, -7 cm, and -4 cm for the 'A, B and C modes', respectively. The typical plasma density and electron temperature at $(r, z) = (0, z_0)$ for an effective rf power of about 600 W are about 4.5×10^{11} cm⁻³ and 4 eV, 5×10^{11} cm⁻³ and 4.5 eV, and 1.5×10^{12} cm⁻³ and 5.5 eV for the 'A, B and C modes', respectively; the rf antenna current is simultaneously measured with the plasma 'on' while performing all experiments to derive the power transfer efficiency [15] and the resultant effective power absorbed into the plasma.

Measurements of T_{total} and T_B are carried out as a function of rf power for cases A-C and for cases A and B, respectively, and the results are shown as open squares and open circles on Fig. 3. The total force T_{total} increases with the effective rf power and reaches a maximum of about 2 mN, 6 mN, and 3.5 mN for all the 'A, B and C modes', respectively. A significant difference in T_{total} between the 'A mode' and the 'B mode' is observed despite their similar maximum densities, electron temperatures, and source radii. The force T_B resulting from the magnetic field increases to about 0.6 mN and 3 mN for the 'A and B modes', respectively; it is found that the large values for T_{total} measured for the 'B mode' result from the large values measured for T_B . The experimental results on Fig. 3 clearly demonstrate the direct measurement of the axial force onto the magnetic field in current-free magnetically expanding plasmas and the subsequent contribution of this force to the total measured force.

The origin of the force onto the magnetic field is now derived from a fluid model. We consider an axisymmetric, magnetically expanding, current-free plasma system. Assuming quasi-neutrality, negligible electron inertia, and cold ions, the radial and axial components of momentum equations for elec-

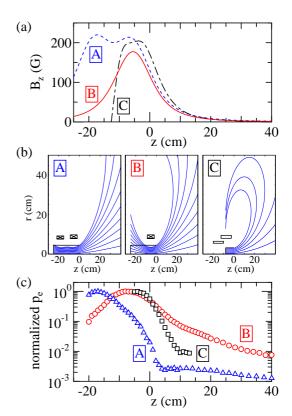


FIG. 2: (a) Axial profiles of the magnetic field B_z on axis for $(I_{Bup}, I_{Bdown}) = (6A, 6A)$ (dotted line), (0A, 6A) (solid line), and the PMs (dotted-dashed line). These are labeled 'A-C modes', respectively. (b)Topologies of the magnetic field lines. The position of the radial wall of the outer chamber is r = 50 cm. (c) Axial profiles of the normalized electron pressure measured on axis for 'A mode' (open triangles, 470 W), 'B mode' (open circles, 540 W), and 'C mode' (open squares, 320 W).

trons and ions in cylindrical coordinates (r, θ, z) are given by

$$-en(E_r + v_\theta B_z) = \frac{\partial p_{e\perp}}{\partial r},\tag{1}$$

$$-en(E_z - v_\theta B_r) = \frac{\partial p_{e\parallel}}{\partial z},\tag{2}$$

$$en(E_r + u_\theta B_z) = 0, (3)$$

$$en(E_z - u_\theta B_r) = \frac{1}{r} \frac{\partial}{\partial r} (rmnu_r u_z) + \frac{\partial}{\partial z} (mnu_z^2),$$
 (4)

where (E_r, E_θ, E_z) , (B_r, B_θ, B_z) , (v_r, v_θ, v_z) , (u_r, u_θ, u_z) , and n are the electric field, magnetic field, electron velocity, ion velocity and plasma density, which are functions of (r, z). e is the elementary charge and m is the ion mass. $p_{e\perp}(r,z) = nk_BT_{e\perp}$ and $p_{e\parallel}(r,z) = nk_BT_{e\parallel}$ are the electron pressures perpendicular and parallel to z, where $T_{e\perp}$ and $T_{e\parallel}$ are the electron temperatures perpendicular and parallel to z, respectively. The radial component of the ion inertia is also neglected as the ions are mainly accelerated along the z axis in this type of plasma system whether by the DL or by ambipolar axial electric fields [16, 17]. By eliminating E_z from Eqs. (2) and (4), a net axial momentum flux $\tau(r,z) \equiv mnu_z^2 + p_{e\parallel}$ per unit cross section, which can be regarded as a pressure, can be given as

$$\frac{\partial \tau}{\partial z} = en(v_{\theta} - u_{\theta})B_r - \frac{1}{r}\frac{\partial}{\partial r}(rmnu_r u_z),\tag{5}$$

where the first term on the RHS is the Lorentz force due to the net azimuthal current and the radial component of the magnetic field. The electron and ion azimuthal currents can be obtained from Eqs. (1) and (3) as $env_{\theta} = -enE_r/B_z - B_z^{-1}\partial(p_{e\perp})/\partial r$ and $enu_{\theta} = -enE_r/B_z$, which correspond to the currents from the electron $\mathbf{E} \times \mathbf{B}$ drift, the electron diamagnetic drift, and the ion $\mathbf{E} \times \mathbf{B}$ drift, respectively. Hence, the net current can be expressed by only the electron diamagnetic current as the $\mathbf{E} \times \mathbf{B}$ drifts cannot drive a net current. When the plasma expands with an axially varying plasma radius $r_p(z)$, and has zero density at $r \geq r_p(z)$, the total axial force $T_{total}(z)$ is given by the volume integration of $\partial \tau/\partial z$ as

$$T_{total}(z) = T_s - 2\pi \int_{z_0}^{z} \int_{0}^{r_p(z)} r \frac{B_r}{B_z} \frac{\partial p_{e\perp}}{\partial r} dr dz$$
$$-2\pi \int_{z_0}^{z} \int_{0}^{r_p(z)} \frac{\partial}{\partial r} (rmnu_r u_z) dr dz, \tag{6}$$

where $T_s = 2\pi \int_0^{r_s} r p_{e\parallel}(r, z_0) dr$ originates from the maximum electron pressure [7] and corresponds to the constant of integration along z when integrating from z_0 . As suggested by Fruchtman, this term is conserved along z even in collisional plasmas [18]. r_s is the source tube radius and the contributions from the magnetic field and the radial source wall upstream of z_0 are not included in Eq. (6) for simplicity. The third term on the right-hand side (RHS) in Eq. (6) presents an axial force delivered by the ions flowing into the radial source wall; it vanishes as the plasma density is assumed to be zero at the plasma edge. The second term on the RHS in Eq. (6) shows the axial force imparted from the Lorentz force and corresponds to the measured force T_B onto the magnetic field (Fig. 3). It results from the azimuthal current $[B_z^{-1}(\partial p_{e\perp}/\partial r)]$ of the electron diamagnetic drift and the radial component (B_r) of the applied magnetic field. Hence, the present theory clearly identifies the gain/loss of the net axial force for negative/positive radial gradient of the electron pressure in an expanding magnetic field in addition to the electron pressure term T_s inside the source tube.

To compare the theory with the experiments, T_B , T_s and $T_{total} = T_s + T_B$ are calculated from Eq. (6) and using the following model of the two-dimensional electron pressure $p_e(r,z)$ along with the two-dimensional magnetic field (B_r, B_z) for the three experimental configurations. To model $p_e(r,z)$, the plasma radius along z is assumed to be determined by the source tube radius as $r_p(z) = r_s$ for $z \le 0$ and by the expanding magnetic field as $r_p(z) = r_s \sqrt{B_z(0,0)/B_z(0,z)}$ [19] for z > 0, and the electron temperature is assumed to be isotropic $(T_{e\perp} = T_{e\parallel})$. The two-dimensional r-z profile of the electron pressure normalized by $p_e(0,z_0)$ is modelled as $p_e(r,z)/p_e(0,z_0) = p_{en}(0,z)f(r,z)$, where $p_{en}(0,z)$ and f(r,z) are the normalized electron pressure along z in Fig. 2(c) and a function giving a radial profile of the normalized electron pressure at z, respectively. f(r,z) for $r \le r_p$ is given by $f(r,z) = 1 - [r/r_p(z)]^{a_1}$ for the 'A and C modes', and by $f(r,z) = a_2\{1 - [r/r_p(z)]^{a_1}\}^{a_3} + (1 - a_2)\{1 - [r/r_p(z)]^{a_4}\}^{a_5}$ for the 'B mode', respectively, and f(r,z) is assumed to be zero for $r > r_p$. a_1 - a_5 are fitting parameters of the electron pressure radial profiles measured at z_0 for 'A-C modes' (not shown here), respectively, and remain unchanged along z. The values of a_1 - a_5 are $a_1 = 5.37$ for A mode, a_1 - $a_5 = 2.07, 3.72, 2.16, 2.89$, and 4.83 for B mode, and $a_1 = 2.07$ for C mode, respectively.

The maximum electron pressures $p_e(0, z_0)$ (plasma density and electron temperature) measured various rf powers are used for the calculation, and the axial integration in Eq. (6) are performed from z_0 to the most downstream positions of the electron pressure measurement (z = 40 cm)for A and B modes, and z = 13 cm for C mode).

The calculated T_B (filled circles), T_s (filled triangles), and T_{total} (filled squares) are plotted in Figs. 3(a)-3(c), respectively, where the dashed, dotted, and solid

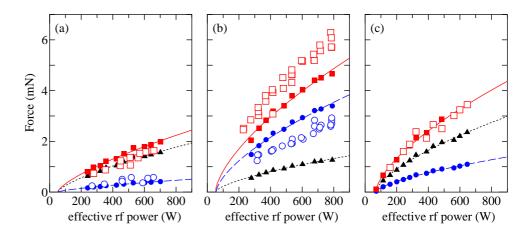


FIG. 3: Directly measured forces T_{total} (open squares) and T_B (open circles) as a function of the effective rf power for the (a) 'A mode', (b) 'B mode', and (c) 'C mode', respectively. The forces T_s (filled triangles), T_B (filled circles), and T_{total} (filled squares) calculated using Eq. (6) are also plotted together with the fitted curves (dotted, dashed, and solid lines) added as visual guides.

lines are fitted curves added as a visual guide. As is seen, the measured momentum fluxes T_B (open circles) and T_{total} (open squares) are in fairly good agreement with the calculated fluxes (filled circles and squares) for all cases tested. This demonstrates that the axial force in an expanding magnetic field can be enhanced as a result of the momentum gain due to the Lorentz force; a force produced due to an electron diamagnetic drift, and the radial component of the magnetic field. As the downstream electron pressure for B mode is larger than that for the other cases, the contribution from the electron diamagnetic effect is greater and gives the larger T_B . The larger discrepancy of about 20 % observed between the theoretical and measured T_{total} and T_B for case B could result from the simplifications related to the radial component of the ion inertial term, the axial force delivered onto the radial source wall, and the two-dimensional profile of the electron pressure.

IV. CONCLUSION

In summary, the direct measurements of the axial force imparted from magnetically expanding current-free plasmas have been performed in three different configurations and compared with a two-dimensional fluid theory. The gain of axial force by the presence of the expanding magnetic field is clearly demonstrated in the experiments. A fluid theory is developed which shows that the axial force is enhanced by the azimuthal current of the electron diamagnetic drift and the radial magnetic field. The directly measured and theoretical forces are in fairly good agreement.

The authors would like to thank Prof. A. Fruchtman of the Holon Institute of Technology for many useful discussions.

- [1] D. L. Meier, S. Koide, and Y. Uchida, Science, 291, 84 (2001).
- [2] T. E. Eastman, Geophys. Res. Lett., 3, 685 (1976).
- [3] A. G. Peeters, C. Angioni, and D. Strintzi, Phys. Rev. Lett., 98, 265003 (2007).
- [4] M. Zuin et al., Phys. Rev. Lett., 92, 225003 (2004).
- [5] A. Sasoh, Phys. Plasmas, 1, 464 (1994)
- [6] H. Tobari, A. Ando, M. Inutake, and K. Hattori, Phys. Plasmas, 14, 093507 (2007).
- [7] A. Fruchtman, Phys. Rev. Lett., **96**, 065002 (2006).
- [8] E. Ahedo, Phys. Plasmas, 18, 033510 (2011).
- [9] E. Ahedo and M. Merino, Phys. Plasmas, 17, 073501 (2010).
- [10] O. V. Batishchev, IEEE Trans. Plasma Sci., 37, 1563 (2009).
- [11] K. Takahashi et al., Appl. Phys. Lett., 98, 141503 (2011).
- [12] S. Pottinger, V. Lappas, C. Charles, and R. Boswell, J. Phys. D: Appl. Phys., 44, 235201 (2011).
- [13] K. Takahashi, T. Lafleur, C. Charles, P. Alexander, and R.W. Boswell, Phys. Rev. Lett., 107, 235001 (2011).
- [14] T. E. Sheridan, Phys. Plasmas, 7, 3084 (2000).
- [15] T. Lafleur, C. Charles, and R. W. Boswell, J. Phys. D: Appl. Phys., 44, 055202 (2011).
- [16] X. Sun et al., Phys. Rev. Lett., 95, 025004 (2005).
- [17] B. W. Longmier et al., Plasma Sources Sci. Technol., 20, 015007 (2011).
- [18] A. Fruchtman, IEEE Trans. Plasma Sci., 36, 403 (2008).
- [19] F. F. Chen, Phys. Plasmas, 13, 034502 (2006).