

1. In high energy plasmas, heavy elements are ionized, and both continuum emission and many emission lines are observed in the X-ray energy band. **(15)**
 - (a) Derive formula of the binding energy of the *hydrogenic ion*, which has only a single electron, of the atomic number Z , using m_e (electron mass), \hbar , e and Z . (5)
 - (b) What is the binding energy of the hydrogenic iron ion (in keV)? (5)
 - (c) Estimate the plasma temperature (in K), where iron is ionized up to hydrogenic ion? (5)
2. Let's consider a spherically radiating star with the mass M . **(20)**
 - (a) Derive the formula of *Eddington luminosity* using c , G , M and κ (mass-absorption coefficient due to Thomson scattering). (10)
 - (b) Estimate typical temperatures (in keV) of "X-ray bursts" and "Super-soft Sources" assuming the blackbody radiation from the neutron star or white-dwarf surfaces, respectively, at Eddington luminosity. (10)
3. Let's consider mass accretion to non-spinning black holes ($a=0$) or maximally spinning black holes ($a=1$). **(20)**
 - (a) What is the Innermost Stable Circular Orbit (ISCO) for each case? (10)
 - (b) Using Newtonian approximation, estimate energy conversion efficiency for each case when materials fall from infinity to ISCO. (Note, the precise values are $1 - \sqrt{8/9}$ ($a=0$) and $1 - \sqrt{1/3}$ ($a=1$) according to the general relativity.) (10)
4. Let's consider standard accretion disks around black holes. **(20)**
 - (a) Estimate innermost temperature (in keV) of the standard accretion disk around a black hole with the mass M , assuming that the disk is radiating with blackbody at Eddington luminosity, and the black hole is not spinning. (10)
 - (b) Estimate the innermost disk temperature of the standard disk around the black holes with $M = 10M_\odot$ and $M = 10^9M_\odot$. Which wave-length would be most appropriate to observe these targets? (10)
5. Let's consider X-ray satellites by JAXA/ISAS (ASCA, Suzaku, Hitomi) which have the telescope in the direction of the satellite Z-axis and the solar-panel in the direction of the Y-axis. The satellite attitude is described with the Z-Y-Z Euler angle. What are the Euler angles to observe North Ecliptic Pole (NEP) region in spring-equinox, summer-solstice, autumn-equinox and winter solstice? **(15)**
6. Let's consider synchrotron radiation or non-thermal inverse-Comptonized radiation from the relativistic electrons whose number density is given as $\propto \gamma^{-p} d\gamma$ in a wide-energy band, where $mc^2\gamma \equiv mc^2/\sqrt{1 - (v/c)^2}$ is the electron energy. In both cases, the following conditions are satisfied;
 - (a) Characteristic photon energy ($\equiv h\nu_c$) emitted from a single electron is proportional to the electron energy ($\propto \gamma^2$).
 - (b) Energy spectrum of photons emitted from a single electron is represented as a function of ν/ν_c . Show that the expected synchrotron radiation and the inverse-Compton radiation have the power-law energy spectra, $\propto \nu^{-s}$, and derive the relation between s and p . **(10)**