

Lesson 6, 7 and 8 (Methods of astronomy and space astronomy)

2023-05-03 11:05

Constellations 星座

- How many constellations are there? 88
- Are the constellation names and their boundaries unambiguously defined? Yes!
- If Yes, who defined them? How can we know that? IAU

Scorpius = 天蝎座

The Constellation by International Astronomical Union (IAU)

- Is the "Crab nebula" (05 38 56.6, -64 05 03.3, ICRS) located in the constellation Crab? No!
Crab nebula with optical (DSS) and X-ray (Chandra) displayed with IPDQ at DARTS/IAU

Expression of the coordinates

- Explain the two expressions to express values of the coordinates. Take an example "Cyg X-1":
(RA, Dec) = (19 58 21.7, +35 12 05.8) or (101.950316, 35.201699) in J2000
19h 58m 21.69s 35° 12' 05.8"
Useful web-tools: SIMBAD, Coordinate Converter, J2002
- What are the conversion formulae between them?

Naming of X-ray sources

- The first celestial X-ray source, Sco X-1, was discovered in 1962. Since then, how are the X-ray sources named?
Cyg X-1, LMC X-1, GX339-4, 1A0620-00, GS1124-08, PSR B1509-58, GRO J1655-40, MAXI J1348-630, etc.
GX339-4 means "Galactic X-ray source at galactic coordinates (l, b) (339, -4)".
X-ray sources around the Galactic Center displayed with IPDQ MAXI and Swift/BAT images, Suzaku pointing fields superposed

Precession of the equinoxes and epoch

- Explain precession of the equinoxes and epoch.
B1950 -> based on the equinox 1950
J2000 -> based on the equinox 2000
- Explain the International Celestial Reference Frame (ICRF) or System (ICRS).
Based on the Barycenter of the solar system -> We do not have to worry about precession of Earth!
- How can we convert B1950 coordinates to J2000 (ICRF) or vice versa?
-> Use COCO, or any converters!

Coordinate conversion

- Explain the three astronomical coordinates, equatorial coordinates, ecliptic coordinates, and Galactic coordinates.
Animation to explain the equatorial to galactic coordinates
- Find (web) tools to carry out these coordinate conversions.
R programs to convert Cyg X-1 equatorial coordinates to ecliptic, or to galactic coordinates
- Write a simple program by yourself to carry out these coordinate conversions.

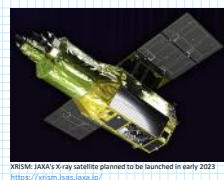
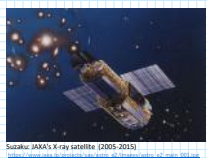
Output of COCO for Cyg X-1

J2000		B1950		Galactic		Ecliptic	
RA	Dec	RA	Dec	l	b	lon	lat
19 58 21.7	+35 12 05.8	19 58 28.87	+35 03 54.5	71 20 04.0	03 04 03.8	313 40 24.7	54 14 44.8
101.950316	35.201699	299.120291	35.085134	71.334900	3.066836	313.673532	54.245772

Handwritten notes: $l = 71.3349$, $b = 3.0668$, $lon = 313.6735$, $lat = 54.2458$

Season and observability

- We would like to observe the famous black hole binaries Cyg X-1 (19 58 21.7, +35 12 05.8, ICRS) and LMC X-3 (05 38 56.69, -64 05 03.3, ICRS) with ground "optical telescopes". Where and when can we observe them?
How many times do we have the "best" observation periods (the target is near the zenith at midnight) per year?
Once (when the source is located opposite to the Sun)
- What if using ground "radio" telescopes?
You may observe in day-time, so you may choose the "best" period all-around year. (However, you may not observe very close to the Sun.)
- What if using "ordinary" astronomical satellites, where the telescope is pointing perpendicular to the "fixed" solar panel? (Sun angle is ~90 degree)
How many times do we have the "best" observation periods (Sun is perpendicular to the solar-panel) per year?
Usually, twice a year, when the target is perpendicular (90 degree apart) to Sun.
If the source is close to NEP or SEP, the source is always observable.



Viewing HELP

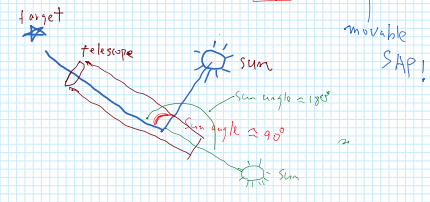
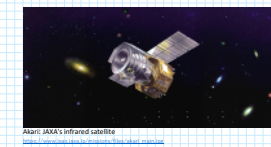
Determine when or if an astronomical position can be viewed by a given space

Select one or more space telescopes:

- Chandra, allowed Sun angle range = 46-170
- HST, allowed Sun angle range = 60-180
- IXPE (planning), allowed Sun angle range = 65-115
- NICER, allowed Sun angle range = 45-180
- NuSTAR, allowed Sun angle range = 43-180
- Swift, allowed Sun angle range = 47-180
- XMM-Newton, allowed Sun angle range = 20-110
- XRISM, allowed Sun angle range = 65-120

Cyg X-1 observation log by Suzaku
LMC X-3 observation log by Suzaku
Cyg X-1 observability by HEASARC's viewing
LMC X-3 observability by HEASARC's viewing

- For most astronomical satellites, where the telescope is pointing perpendicular to the "fixed" solar panel, there are two locations on the sky which are always observable. Where are they (their coordinate in the equatorial coordinates is)?



The ASCA Slow survey

XMM-Newton satellite slow track (in galactic coordinates)

All-sky survey (from you tube)

Rosetta (launched in 2019), exposure map (in equatorial coordinates)

Rosetta mosaic by DLR (from you tube)

Satellite Attitudes and observing targets

Below, we consider astronomical satellites where the spin axis is Z-axis and the solar panel is toward Y-axis, and the telescope is along the X-axis, which is toward the observing target.

The "Euler angles" to describe the satellite attitude are defined as sequential rotation around Z, Y, X axes, (θ, φ, ψ).

1. Express the 3D rotation matrix using the Euler angles (θ, φ, ψ).

$$R = R_z(\theta) R_y(\phi) R_x(\psi)$$

$$R_z(\theta) = \begin{pmatrix} \cos \theta & 0 & 0 \\ 0 & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$R_y(\phi) = \begin{pmatrix} \cos \phi & 0 & \sin \phi \\ 0 & 1 & 0 \\ -\sin \phi & 0 & \cos \phi \end{pmatrix}$$

$$R_x(\psi) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \psi & \sin \psi \\ 0 & -\sin \psi & \cos \psi \end{pmatrix}$$

3x3 orthogonal matrix
Sky coordinates → satellite coordinates

- Explain the relationship between the Euler angles and the satellite attitude

- Explain the relationship between the first two Euler angles (θ, φ) and the equatorial coordinates of the observing target (l, b).

ASCA observation report on 1993/05/11

Time	RA	Dec	RA	Dec	RA	Dec
00:00:00	19 58 21.7	+35 12 05.8	19 58 21.7	+35 12 05.8	19 58 21.7	+35 12 05.8

Object Name or Coordinates (e.g., Cyg X-1 or 101.295, -16.699 or 6)

Select Coordinate System: J2000

Name Resolvers: ORL, then SIMBAD else VizieR (Default), then NEO

Special Spaces: Use local caches

Find Target Convert Coordinates [Reset]

Target MS1 resolved by SIMBAD (local cache)

J2000	B1950	Galactic	Ecliptic		
RA	Dec	l	b	lon	lat
19 58 21.7	+35 12 05.8	71 20 04.0	03 04 03.8	313 40 24.7	54 14 44.8

φ = RA
θ = 90 - Dec

3. Explain the relationship between the third Euler angle and the "roll angle" of the observation. (See the [power point file](#) to illustrate the relationship)

5. North Ecliptic Pole (NEP) and South Ecliptic Pole (SEP) are observable all around the year. What are the Euler angles to observe NEP and SEP in Spring equinox, Summer solstice, Autumn equinox and Winter solstice.

	NEP (270, 66.6)	SEP (90, -66.6)
Spring	(270, 23.4, 0)	(90, 156.6, 180)
Summer	(270, 23.4, 90)	(90, 156.6, 90)
Autumn	(270, 23.4, 180)	(90, 156.6, 0)
Winter	(270, 23.4, 270)	(90, 156.6, 270)

6. The Suzaku satellites observed the NEP region several times at different seasons. Using [JMOD](#), see how the roll angle changes with seasons.

Satellite attitudes and quaternion (q-parameters)

Look at an example of the ASCA satellite attitude file (on the right-hand side), where four numbers are given every 0.5 sec.

An example of ASCA attitude file, taken from https://data.darts.isas.jaxa.jp/pub/asca/asca_rev07/10010100/asa/asa0907_09310418.asc

1. Calculate the "norm" of these four numbers. What are these numbers?

Line quaternion (単位四元数)

```

TIME          QPARSAM
8.303603855937183E+06 -4.2141317818602299E-01
-3.67162842241615E-01
-6.068271680427795E-01
6.65121897661020E-01
8.30360355954587E+06 -4.214131578433074E-01
-3.67143576955380E-01
-6.068260876402793E-01
6.651171313420200E-01
8.303603855931759E+06 -4.214093076129627E-01
-3.671629415753114E-01
-6.06826148901474E-01
6.65113376309049E-01
8.303604355949163E+06 -4.21407973178000E-01
-3.671884697731878E-01
-6.0682608128972E-01
6.651161091929086E-01
    
```

4. What is the merit of using quaternion to describe satellite attitudes (or any 3D rotations) instead of Euler angles?

The rotation axis and angle are directly given from quaternion.

5. Carry out a single rotation around a rotation axis from equatorial coordinate to Galactic coordinate using quaternion?

Animation to illustrate the Euler rotation

Animation to illustrate the single rotation

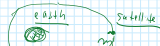
6. How can we perform satellite maneuver from the attitude described by the quaternion "q" to the one described by "q'?"

The new quaternion "qp-1" gives the maneuver from "q" to "q", defining the rotation axis and the rotation angle.

Animation to illustrate the satellite attitude maneuver from "q" to "q'?"

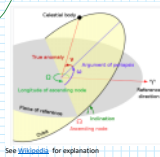
7. How can we "average" two satellite attitudes?

Carry out a half rotation around that axis.



Satellite orbits, orbital six parameters, Two Line Elements (TLE)

1. Name each axis (a)
2. Eccentricity (e)
3. Inclination (i)
4. Longitude of the ascending node (Ω)
5. Argument of periastron (ω)
6. True anomaly at the Epoch.



3D diagram to explain the satellite orbits in my home page; to demonstrate difference of inclination [click here](#)

2. Where are the Two Line Elements (TLE)? Where can we find them?

Go to NORAD!

<https://www.cesr.cnr.it/NORAD/tlelements/>

See [Wikipedia](#) for explanation

A line explanation in Japanese by Isana-san

[Orbits of major high-energy satellites](#) (thanks to Isana-san)

[Orbits of ASTRO-in \(Arinon\) and its debris](#)

SUZAKU (ASTRO-E11)
 1 28773U 05025A 21151.54108102 00001204 00000-0 52851-4 0 9982
 2 28773 31.3815 272.0277 0004320 113.3039 246.8063 15.16381444876591

<https://satellite.ku.edu/control/isa/isa/ASTRO-E11/>

Orbits and astronomical objects

1. Where can we find orbital elements of solar planets and asteroids?

Go to JPL to obtain the orbital six parameters (six parameters) [for planets](#) or [for asteroids and comets](#)

2. Find orbital elements of your familiar/favorite asteroids.

3. Are there asteroids which have your name?

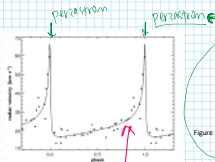
4. Give some examples of binary stars where elliptical orbits affect their emission?

```

#name# eqprv  N  DTG  TLE1#  TLE2#  TLE3#
#001# Terzan  02089  1  0.00788  0.01782027  - 27283  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#002# Terzan2  02089  1  0.00788  0.01782027  - 27284  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#003# Terzan3  02089  1  0.00788  0.01782027  - 27285  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#004# Terzan4  02089  1  0.00788  0.01782027  - 27286  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#005# Terzan5  02089  1  0.00788  0.01782027  - 27287  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#006# Terzan6  02089  1  0.00788  0.01782027  - 27288  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#007# Terzan7  02089  1  0.00788  0.01782027  - 27289  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#008# Terzan8  02089  1  0.00788  0.01782027  - 27290  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#009# Terzan9  02089  1  0.00788  0.01782027  - 27291  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#010# Terzan10 02089  1  0.00788  0.01782027  - 27292  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#011# Terzan11 02089  1  0.00788  0.01782027  - 27293  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#012# Terzan12 02089  1  0.00788  0.01782027  - 27294  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#013# Terzan13 02089  1  0.00788  0.01782027  - 27295  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#014# Terzan14 02089  1  0.00788  0.01782027  - 27296  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#015# Terzan15 02089  1  0.00788  0.01782027  - 27297  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#016# Terzan16 02089  1  0.00788  0.01782027  - 27298  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#017# Terzan17 02089  1  0.00788  0.01782027  - 27299  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#018# Terzan18 02089  1  0.00788  0.01782027  - 27300  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#019# Terzan19 02089  1  0.00788  0.01782027  - 27301  17.40133  120.00891  11.262819  12.00  0.13  20. 00
#020# Terzan20 02089  1  0.00788  0.01782027  - 27302  17.40133  120.00891  11.262819  12.00  0.13  20. 00
    
```

Congratulations Tanaka-san, Suzuki-san and Satoru/Satoshi-san! There are asteroids having your names!

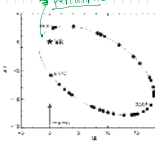
WR140



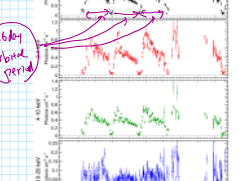
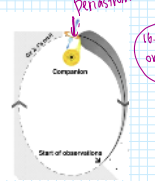
WR140 orbit movie by TLEP

WR140 simulation movie by Chikazaki-san

Figure from <https://www.aanda.org/articles/aa/pdf/2001/35/aa02722.pdf>



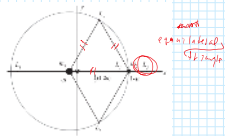
CX-1



<http://www.saii.isas.ac.jp/research/isa/satellite/2012/sum04/CX-1%20X-1%20talk.pdf>

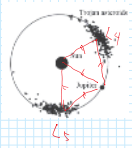
The circular restricted three-body problem and the Lagrange points

1. Explain the circular restricted three-body problem and the Lagrange points



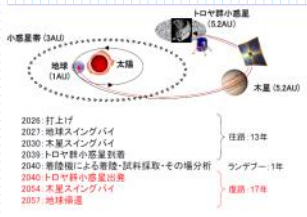
Figures taken from <https://www.ias.ac.in/article/full/iasa/03/02/02-033.pdf/char/2>

2. What are the "Trojan asteroids"?



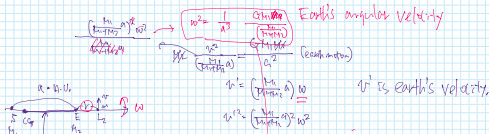
3. Do we have a plan to reach and study Trojan asteroids?

Yes! OKEANOS project



https://www.researchgate.net/publication/341810581/figure/fig/1/figure-fig1/1516116118/oc_session-6035a3a13magnuof1c0z0oc

4. Consider the Sun-Earth L2 point. Let's put the Solar mass M_1 , Earth mass M_2 , their distance a , and the distance between the earth and the L2 is r . What will be the equation of the motion at L2?



5. Solve the equation of motion, and estimate the distance between the earth and L2.

$r \approx 0.01a$

Earth's angular velocity $\omega^2 = \frac{GM_1}{a^3}$

$\omega^2 = \frac{GM_1}{a^3} = \frac{GM_1}{(a+r)^3}$ (approx. same)

$v^2 = \left(\frac{GM_1}{a}\right)\omega$ v^2 is earth's velocity

$\omega^2 = \left(\frac{GM_1}{(a+r)^3}\right)\omega$

Equation of motion @ L2 (lead to eliminate v^2)

Earth and L2 have the same angular velocity ω

$M_2 \approx 10^{-3} M_1$
 $a \approx 1.5 \times 10^8 \text{ km}$ use this approximation

equation of motion @ L2

$\frac{GM_1}{a^3} \left(r + \frac{M_1}{M_1+M_2} a \right) = \frac{GM_1}{(a+r)^3} + \frac{GM_2}{r^2}$

$\frac{1}{a^3} (M_1+M_2) + \frac{M_2}{a^3} = \frac{M_1}{a^3(1+r/a)^3} + \frac{M_2}{r^2}$

$\frac{r}{a^3} \left(1 + \frac{M_2}{M_1} \right) + \frac{1}{a^3} = \frac{1}{a^3(1+r/a)^3} + \frac{1}{r^2} \frac{M_2}{M_1}$

$\left(\frac{r}{a}\right) \left(1 + \frac{M_2}{M_1}\right) + 1 = \frac{1}{\left(1 + \frac{r}{a}\right)^3} + \left(\frac{a}{r}\right)^2 \frac{M_2}{M_1}$

$\left(\frac{r}{a}\right) \cdot \left(1 + \frac{10^{-3}}{1}\right) \cdot \left(1 + \frac{10^{-3}}{1}\right) + 1 + 2\left(\frac{r}{a}\right)^2 = \frac{1}{\left(1 + \frac{r}{a}\right)^3} + \frac{10^{-2}}{10^2} \frac{M_2}{M_1}$

Point 1!
Leave value $\sim 10^{-2} / 10^2$

$= 1 + \left(1 + \frac{2}{10^2}\right) \left(\frac{r}{a}\right)^2 + 2\left(\frac{r}{a}\right)^2$

$3\frac{r}{a} = \left(\frac{10^{-2}}{1}\right) \left(\frac{M_2}{M_1}\right)$

$3\left(\frac{r}{a}\right)^3 = \frac{M_2}{M_1}$

$r = a \left(\frac{M_2}{3M_1}\right)^{\frac{1}{3}}$
 $= a (10^{-3})^{\frac{1}{3}}$
 $\approx 10^{-2} a$

$M_1 = 2 \times 10^{30} \text{ kg}$
 $M_2 = 6 \times 10^{24} \text{ kg}$
 $\frac{M_2}{M_1} = 3 \times 10^{-6}$

Satellite orbits around the L2 point

1. Give several examples of the science satellites (space crafts) which are launched to Sun-Earth L2 point?

- [Planck orbit](#)
- [Mars Reconnaissance Orbiter \(MRO\)](#)
- [ESA's Euclid](#) (ESA's mission's presentation at 2020 SPIE) Explanation of the orbit starting at about 5:40

2. What will be the orbit like around L2? How does it called?

Lissajous orbit

- [Mission for Point Foresee - a Study in Day Television](#)
- [L2 orbit](#) (nice movie and explanation)